

WORKSHEET CHAPWISE - 1

12th Standard CBSE

Maths
Relations and Functions

Total Mark : 39

1 Mark Questions

5 x 1 = 5

- 1) Given set $A = \{a, b, c\}$. An identity relation in set A is
(a) $R = \{(a, b), (a, c)\}$ (b) $R = \{(a, a), (b, b), (c, c)\}$ (c) $R = \{(a, a), (b, b), (c, c), (a, c)\}$ (d) $R = \{(c, a), (b, a), (a, a)\}$
- 2) Given triangles with sides $T_1 : 3, 4, 5$; $T_2 : 5, 12, 13$; $T_3 : 6, 8, 10$; $T_4 : 4, 7, 9$ and a relation R in set of triangles defined as $R = \{(\Delta_1, \Delta_2) : \Delta_1 \text{ is similar to } \Delta_2\}$. Which triangles belong to the same equivalence class?
(a) T_1 and T_2 (b) T_2 and T_3 (c) T_1 and T_3 (d) T_1 and T_4
- 3) A relation S in the set of real numbers is defined as $xSy \Rightarrow x - y + \sqrt{3}$ is an irrational number, then relation S is
(a) reflexive (b) reflexive and symmetric (c) transitive (d) symmetric and transitive
- 4) Let R be a relation on the set L of lines defined by $l_1 R l_2$ if l_1 is perpendicular to l_2 , then relation R is
(a) reflexive and symmetric (b) symmetric and transitive (c) equivalence relation (d) symmetric
- 5) Given set $A = \{1, 2, 3\}$ and a relation $R = \{(1, 2), (2, 1)\}$, the relation R will be
(a) reflexive if $(1, 1)$ is added (b) symmetric if $(2, 3)$ is added (c) transitive if $(1, 1)$ is added
(d) symmetric if $(3, 2)$ is added

2 Mark Questions

5 x 2 = 10

- 6) Define symmetric Relation. Give one example
- 7) Define Transitive Relation. Give one example.
- 8) Given an example of a relation which is
(i) Reflexive, Symmetric and transitive
(ii) Reflexive, Symmetric and not transitive.
- 9) Define Reflexive. Give one example.
- 10) Let $f: X \rightarrow Y$ be a function Define a relation R on X given by $R = \{(a, b) : f(a) = f(b)\}$ Show that R is an equivalence relation ?

4 Mark Questions

5 x 4 = 20

- 11) Show that the relation R defined by $(a, b) R (c, d) \Rightarrow a + d = b + c$ on the set $N \times N$ is an equivalence relation.

12) Let $f: \mathbb{N} \rightarrow \mathbb{N}$ be defined by $f(n) = \begin{cases} \frac{n+1}{2}, & \text{if } n \text{ is odd.} \\ \frac{n}{2}, & \text{if } n \text{ is even} \end{cases}$ for all $n \in \mathbb{N}$. State whether the function f is onto, one-one or bijective. Justify your answer.

13) Prove that the relation R in the set $A = \{1, 2, 3, 4, 5\}$ given by $R = \{(a, b) : |a - b| \text{ is even}\}$, is an equivalence relation.

14) Let Z be the set of all integers and R be the relation on Z defined as $R = \{(a, b) : a, b \in Z, \text{ and } (a - b) \text{ is divisible by } 5\}$. Prove that R is an equivalence relation.

15) Let T be the set of all triangles in a plane with R a relation in T given by $R = \{(T_1, T_2) : T_1 \text{ is congruent to } T_2 \text{ and } T_1, T_2 \in T\}$. Show that R is an equivalence relation.

4 Mark Questions

1 x 4 = 4

16) A relation R on a set A is said to be an equivalence relation on A iff it is

(a) Reflexive i.e., $(a, a) \in R \forall a \in A$

(b) Symmetric i.e., $(a, b) \in R \Rightarrow (b, a) \in R \forall a, b \in A$

(c) Transitive i.e., $(a, b) \in R$ and $(b, c) \in R \Rightarrow (a, c) \in R \forall a, b, c \in A$

Based on the above information, answer the following questions.

(i) If the relation $R = \{(1, 1), (1, 2), (1, 3), (2, 2), (2, 3), (3, 1), (3, 2), (3, 3)\}$ defined on the set $A = \{1, 2, 3\}$, then R is

(a) reflexive (b) symmetric (c) transitive (d) equivalence

(ii) If the relation $R = \{(1, 2), (2, 1), (1, 3), (3, 1)\}$ defined on the set $A = \{1, 2, 3\}$, then R is

(a) reflexive (b) symmetric (c) transitive (d) equivalence

(iii) If the relation R on the set \mathbb{N} of all natural numbers defined as $R = \{(x, y) : y = x + 5 \text{ and } x < 4\}$, then R is

(a) reflexive (b) symmetric (c) transitive (d) equivalence

(iv) If the relation R on the set $A = \{1, 2, 3, 13, 14\}$ defined as $R = \{(x, y) : 3x - y = 0\}$, then R is

(a) reflexive (b) symmetric (c) transitive (d) equivalence
